

Is my teaching innovative ... or just a good craftmanship?

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Vienna University of Technology, Austria

DIAM, Gdańsk, 24th of June 2024

Charles Church and TU Wien



Content

Tell me, and I'll forget it.

Show me, and I'll remember.

Let me do it, and I'll keep it.

Konfuzius



Content

- ▶ **University teaching: a challenge!**
- ▶ University teacher / student – a changing relationship:
 - Lecture/Tutorial: Linear Algebra f. TPH
 - Tutorial: Computernumerics f. TPH
- ▶ Summary

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General framework

School/University: What is different?

- Fundamental assumption:
Voluntary participation and interest in the subject.
- Teaching is **not the only task** of the university teachers.
- **Large number** of students in the class.

Consequences for the students:

- Freedom, not known in the school.
- Great independence required (information).
- Communication is more difficult, psychological barrier.

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Teaching: A challenge!

Consequences for the university teachers:

Is teaching important to me?

Do I have enough time?

- Arouse interest and enthusiasm. Motivation.
- Convey the feeling that students are important to you.
- Facilitate understanding: apply the theory, use the tools that reinforce the insights, visualize wherever possible.
- Enable the smooth running of the course. Provide complete information in time.
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Lecture/Tutorial: Linear Algebra f. TPH

'Matrix' is all you need!



Lecture/Tutorial: Linear Algebra f. TPH (2)



Linear Algebra f. TPH

- Introductory mathematical course in the curriculum for TPH, 1. term, for approx. 300 persons.
- Topics: Basic concepts (vector spaces, linear independence, basis, dimension), linear systems of equations (matrix as linear operator acting between vector spaces), Euclidean spaces, eigenvalue problems, ordinary differential equations.
- Length: 2 hours per week.
- Large lecture hall, touchscreen laptop, projecting the printed lecture notes and a document with notes written during the lecture (uploaded).
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Information:

- TISS information system:
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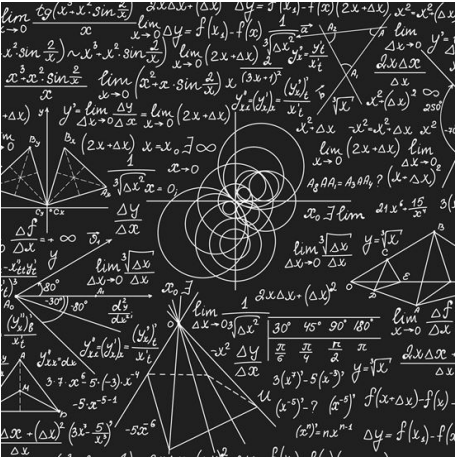
Introduction



Introduction

There is no science that has not developed from the knowledge of phenomena, but in order to benefit from this knowledge, one has to be a mathematician.

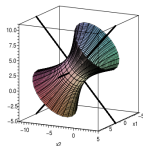
Daniel Bernoulli



Lecture notes

LINEARE ALGEBRA für TPH

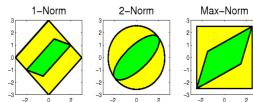
Winfried Auzinger
Gabriela Schranz-Kirlinger
Peter Szmolyan
Ewa Weinmüller



Wien, 2020

ÜBUNGSSKRIPTUM zur LINEAREN ALGEBRA für TPH

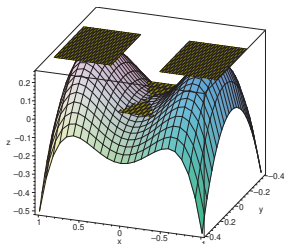
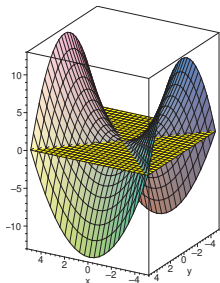
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Wien 2019

During the course

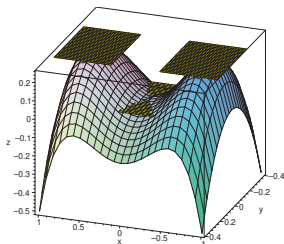
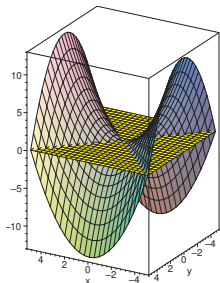
- Graphical illustration whenever possible.



- Relate mathematical notions to their physical applications.
Work \Leftrightarrow line integral of a vector field.
- Touchscreen laptop, projecting the printed lecture notes and a document with notes written during the lecture (uploaded).
- Illustration videos on YouTube: 3Blue1Brown Essence of linear algebra
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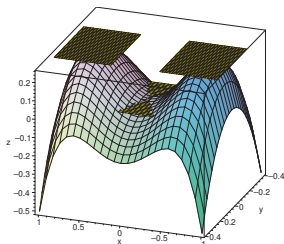
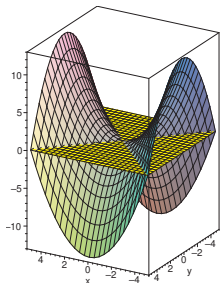
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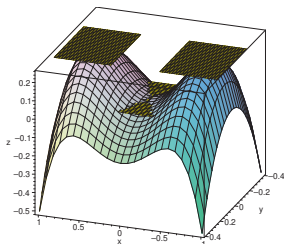
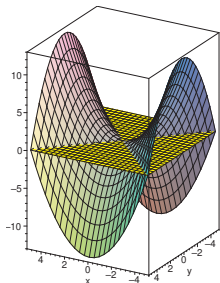
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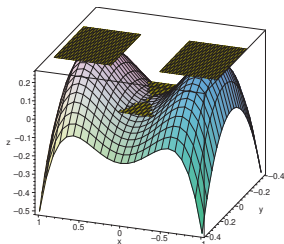
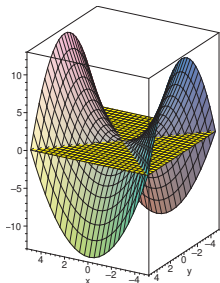
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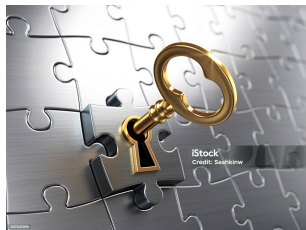
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Closing lecture



Part 1: Highlights: Principles, concepts, results, solution methods... trying to give a weighting.

Part 2: My research area: Numerical Analysis, Scientific Computing ... steam generator.

Part 3: Still something missing?

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- **Lecture/Tutorial: Computer Numerics (for applied sciences 2 hours/week)**
- Approximation for $\pi = 3.141592\dots$
- Archimedes: Consider a unit circle, its circumference is $C_{\text{circle}} = 2\pi$. Consider the inscribed and the circumscribed hexagon:

Closing lecture: Part 3

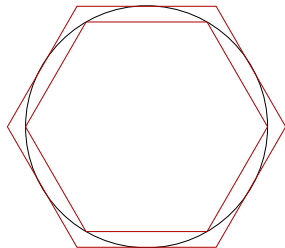
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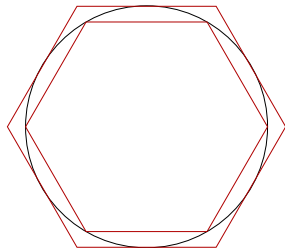


$$C_K < C_{\text{circle}} < C_K$$

$$\frac{C_K}{2} < \pi = \frac{C_{\text{circle}}}{2} < \frac{C_K}{2}$$

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$$C_k < C_{\text{circle}} < C_k$$

$$\frac{C_k}{2} < \pi = \frac{C_{\text{circle}}}{2} < \frac{C_k}{2}$$

$$3\frac{10}{71} < \pi < 3\frac{1}{7} \Rightarrow \pi \approx 3.141831107$$

Closing lecture: Part 3

$$u_1 := 2, \quad u_{k+1} := 2^{k+1} \sqrt{2 \left(1 - \sqrt{1 - (2^{-k} u_k)^2} \right)}, \quad k = 1, 2, \dots$$

2	2.828427124746190
4	3.1 21445152258053
6	3.14 0331156954739
8	3.1415 13801144146
10	3.1415 87725279961
12	3.141592 345611077
14	3.1415926 33463248
16	3.1415926 45321215
18	3.141592 910939673
20	3.14159 6553704820
22	3.141 674265021758
24	3.14 2451272494134
26	3.1 62277660168380
30	0.0000000000000000 !!!

Closing lecture: Part 3

$$u_1 := 2, \quad u_{k+1} := u_k \sqrt{\frac{2}{1 + \sqrt{1 - (2^{-k} u_k)^2}}}, \quad k = 1, 2, \dots$$

2	2.828427124746190
4	3.1 21445152258053
6	3.14 0331156954753
8	3.141 513801144301
10	3.1415 87725277160
12	3.14159 2345570118
14	3.1415926 34338563
16	3.14159265 2386591
18	3.1415926535 14593
20	3.14159265358 5094
22	3.141592653589 501
24	3.1415926535897 76
26	3.14159265358979 4
28	3.14159265358979 5
30	3.14159265358979 5

Computernumerics

```
DO 300 J=JMIN-1,JM/
300   TSOL(J)=15.(
      TRHS(JMIN)=4.000
      TRHS(JMAX)=6.000
DO 400 J=JMIN+1,JM/
400   TRHS(J)=5.0(
      WRITE(6,410)
      WRITE(6,420) (TSOL
410   FORMAT(' DIE STARTI
420   FORMAT(1H ,7F7.2)
C
C   berechnung des res
C
      CALL R E S G (TSOL
      CALL A U S G V (RE
C
C   berechnung der jac
C
      CALL J A C (TSOL(JI
      CALL A U S G M (A(
C
C   loesung des linearen gleichungssystems a(tsol)delta=-res(tsol);
C   parameterbeschreibung f"ur lsarb findet man in der imsl library
C
      CALL D L S A R B (JMAX-JMIN+1,A(1,JMIN),3,1,1,RES(JMIN),1,
&DELTA(JMIN))
C
C   berechnung der neuen loesung nsol(j), j von jmin-1 bis jmax+1, und
C   deren ausgabe
C
      NSOL(JMIN-1) = TSOL(JMIN-1)
      NSOL(JMAX+1) = TSOL(JMAX+1)
DO 500 J=JMIN,JMAX
500   NSOL(J)=TSOL(J)+DELTA(J)
      WRITE(6,600)
      WRITE(6,610) (NSOL(J),J=JMIN-1,JMAX+1)
600   FORMAT(' DIE NEUE LOESUNG DES LINEARISIERTEN PROBLEMS')
```



Tutorial for Computernumerics



Tutorial for Computernumerics

- 4th term, 72 participants
- 2 projects pro term, one topic for a small group of 6, three subtopics for 3 pairs \Rightarrow 36 pairs
- one meeting per week, 30-45 minutes per group \Rightarrow 6 to 9 hours per week
- written documentation in Latex

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